Pair breaking and Coulomb effects in cold fission from reactions

 $^{233}\mathrm{U}(\mathrm{n}_{th},\!\mathrm{f}),~^{235}\mathrm{U}(\mathrm{n}_{th},\!\mathrm{f})$ and $^{239}\mathrm{Pu}(\mathrm{n}_{th},\!\mathrm{f})$

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Abstract

In this paper, the distribution of mass and kinetic energy in the cold region of the thermal neutron induced fission of 233 U, 235 U and 239 Pu, respectively, is interpreted in terms of nucleon pair-breaking and the Coulomb interaction energy between complementary fragments (Coulomb effect). The fission process ends in the scission configuration, in which complementary fragments 1 and 2, having proton numbers Z_1 and Z_2 , and mass number A_1 and A_2 , only interact each other with electrostatic repulsion, by what each one acquires kinetic energy E_1 and E_2 , respectively. However, before reach detectors, they emit n_1 and n_2 neutrons. Thus, the final detected fragments have mass numbers m_1 (= $A_1 - n_1$) and m_2 (= $A_2 - n_2$), and kinetic energies e_1 (= $E_1[1 - n_1/A_1]$) and e_2 (= $E_2[1 - n_2/A_2]$), respectively. In order to avoid the erosive consequences of neutron emission, one studies the cold fission regions, corresponding to total kinetic energy (TE) close to the maximum available energy of the reaction (Q). Contrary to expected, in cold fission is not observed high odd-even effect in mass number distribution. Nevertheless, the measured values are compatible with higher odd-even effects on proton or neutron number distribution, respectively. In addition, in cold fission, the minimal total excitation energy (X) is correlated with the "Coulomb energy excess" (δC) , which is defined as the difference between C (the electrostatic interaction energy between complementary fragments taken as spherical in scission configuration) and Q. These Coulomb effects increase with the asymmetry of the charge fragmentations. In sum, the experimental data on cold fission suggest that scission configurations explore all the possibilities permitted by the available energy for fission.

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I. INTRODUCTION

Among the most studied properties of the nuclear fission of actinides are the distributions of mass, charge and kinetic energy associated to complementary fragments. However, R. Brissot et al. [1] observed that the neutron emission from the fragments, occurred before they reach the detector, generates a structure on the final kinetic energy distribution as a function of mass, non-existent on primary fragment distribution. Naturally, neutron emission also erodes odd-even effects on neutron number distribution and consequently on mass number distribution associated to fragments. For these reasons, cold fission regions, corresponding to high kinetic energy associated to fragments that do not emit neutrons, are studied. In that sense, in this paper, mass, charge and kinetic energy distribution in the cold regions from thermal neutron induced fission of 233 U, 235 U and 239 Pu, namely 233 U(n_{th} ,f), 235 U(n_{th} ,f) and 239 Pu(n_{th} ,f), respectively, is interpreted in terms of nucleon pair breaking and Coulomb interaction energy between fragments in scission configuration.

Let us suppose that the complementary fragments have kinetic energies E_1 and E_2 , referred to primary mass numbers A_1 and A_2 , and proton numbers Z_1 and Z_2 , respectively. After the neutron emission, complementary fragments 1 and 2 end with mass numbers

$$m_1 = A_1 - n_1$$

and

$$m_2 = A_2 - n_2$$

where n_1 and n_2 are the numbers of neutrons emitted by the fragments 1 and 2, respectively. The corresponding values of the final kinetic energy associated to those fragments are

$$e_1 \cong E_1 \left(1 - \frac{n_1}{A_1} \right),$$

and

$$e_2 \cong E_2 \left(1 - \frac{n_2}{A_2} \right).$$

In the case that only one of the complementary fragments is detected, which is what happens in the Lohengrin spectrometer at the High Flux Reactor (HFR) of the Laue-Langevin Institute (ILL) in Grenoble [1], subscripts are omitted. For a given primary mass number (A), the kinetic energy (E) distribution is characterized by the corresponding average,

 $\overline{E}(A)$, and standard deviation, $\sigma_E(A)$.

Using the Lohengrin spectrometer in the HFR of ILL in Grenoble, R. Brissot et. al. measured $\overline{e}(m)$ y $\sigma_e(m)$ values in $^{235}\mathrm{U}(n_{th},\mathrm{f})$. Their experimental curve $\sigma_e(m)$ showed a peak around m=110, as it had been predicted by a Monte Carlo simulation performed before that the experiment was carried out. In this simulation it was demonstrated that that broadening e(m) distribution is due to the neutron emission and the sharp fall on $\overline{E}(A)$ in the mass region around m=110. For each mass number m, the kinetic energy distribution is the result of superposition of distributions associated to fragments having $A \geq m$ [1].

In the final mass region $106 \leq m \leq 112$, \overline{e} falls sharply, about 4 MeV per mass number. Let us suppose that the \overline{E} behaviour is similar to that of \overline{e} , and $\sigma_E(A)$ is flat (equal to 5 MeV, for example). Therefore, the average kinetic energies associated to fragments with A=112 is 8 MeV lower than that of fragments associated to A=110. Fragments with A=110, that do not emit neutrons, have the high values of their distribution of primary energies (E); and fragments associated to A=112, that do emit 2 neutrons, have the low E values of their corresponding primary distribution, whose average is already 8 MeV lower than that associated to A=110. Both fragments, one with primary mass numbers 110 y and the other with 112, respectively, having E values with average differences of around 8 MeV, end with m=110. The superposition of these dispersed values contributes with the widening of $\sigma_e(m)=110$.

D. Belhafaf *et.* al., repeating the experiment on $^{235}\text{U}(n_{th},f)$ made by R. Brissot *et.* al. [1], observed a broadening of the distribution of e around m=126 [2]. Moreover, for $^{233}\text{U}(n_{th},f)$, those authors observe a broadening of the distribution of e around m=124. Their simulation did not reproduce these experimental results [2].

For 233 U(n_{th},f) H. Faust *et. al.* [3], using theoretical models on fission dynamics, calculated the distribution of E as a function of A, but not around A = 124. However the D. Belhafaf *et. al.* experimental results for both, 233 U(n_{th},f) and 235 U(n_{th},f), were reproduced by a Monte Carlo simulation performed by de M. Montoya *et. al.* [4, 5]. These

authors shows that the broadening on the distribution of e is generated by the superposition of the distributions of E corresponding to $A \ge m$. For the case of $^{235}\text{U}(n_{th},f)$, \overline{e} falls from 88 MeV referred to m=125, to 84 MeV referred to m=126, while in this region the tendency of \overline{e} is to increase with m [2]. See Fig. 1. It is reasonable to assume that for A near but higher than 126, \overline{E} has a similar behavior. Thus, the superposition E values, corresponding to primary mass numbers $A \ge 126$, having dispersive behavior, contribute to the broadening of e(m) distribution around m=126.

II. NEUTRON EMISSION AND ODD-EVEN EFFECTS IN COLD FISSION

The odd-even effect on the fragment mass number distribution (δA) is defined by the relation:

$$\delta A = \frac{Y_{A_e} - Y_{A_o}}{Y_{A_e} + Y_{A_o}}$$

where Y_{A_e} and Y_{A_o} are yields associated to fragments having even and odd mass numbers, respectively.

Similarly, we define the odd-even effects δN and δZ on the distribution of neutron number (N) and proton number (Z), respectively.

For low energy fission of actinides, the odd-even effect on the proton number distribution of the fragments, previously found to A. L. Wahl *et. al.* [6] and G. Mariolopoulos *et. al.* [7], suggested that must exist high odd-even effects on the mass number distribution, but they are eroded by neutron emission.

To study the mass number distributions undisturbed by the emission of neutrons, C. Signarbieux et. al. chosen high kinetic energy windows associated to fragments from $^{233}\text{U}(n_{th},f)$, $^{235}\text{U}(n_{th},f)$ and $^{239}\text{Pu}(n_{th},f)$, respectively. The number of events analyzed were 1.5×10^6 , 3×10^6 and 3.2×10^6 , respectively. These authors used the difference of time of flight technique to separate fragment mass numbers, with solid detectors to measure the fragment kinetic energy. The experiment was conducted in the HFR of ILL in Grenoble [8, 9].

Although δA is not zero, it is not as high as was expected. However, one may show

that this small δA is compatible with nucleon pair breaking and higher odd-even effects in the distribution of proton or neutron numbers.

H.-G. Clerc *et.* al. [10], for E=114.1 MeV, obtained the mass number distribution presented in Fig. 2, from which one calculates $\delta A=30.14$ %. The mass number distribution in the window of light fragment kinetic energy 113.5 < E < 114.5 MeV, in 233 U(n_{th},f), is presented in Fig. 3 [9]. From this distribution one gets $\delta A=32.18$ %.

In order to interpret values of δA , δZ and δN , lets first define, for each A, Z_0 as the light fragment proton number that corresponds to maximal available energy of the reaction (Q) Suppose that nucleon pair-breaking occurs, but fragment couple reaching maximum total kinetic energy still corresponding to Z_0 ; therefore, for 233 U(n_{th},f), $\delta Z = 66.6$ % and $\delta N = 33.3$ %. This result is coherent with the stereographic projection of the values obtained by U. Quade *et. al.* [11] for lower energy windows, as it is presented in Figs. 4 and 5.

For total kinetic energy $TE \ge 204$ MeV, only ¹⁰⁴Mo ($Z=42,\ N=62$) survives [9]; therefore $\delta A=1$.

The mass number distribution for the kinetic energy window 113.5 < E < 114.5 MeV, for light fragments from the reaction 235 U(n_{th},f), is presented in Fig. 6, from which one calculates $\delta A = 15.3$ %. For E = 113.7 MeV, W. Lang et. al. obtained the distribution presented in Fig. 7, from which one calculates $\delta A \cong 23.82$ %. For E = 108 MeV, W. Lang et. al. obtain $\delta A \cong 0$, $\delta Z \cong 35$ % and $\delta N \cong 8$ % [12]. Suppose that proton number correspond to Z_0 , then one calculates $\delta Z = 66.6$ % and $\delta N = 33.3$ %. This result is coherent with the stereographic projection of the values obtained by W. Lang et. al. [12] for windows of lower energies, as it is shown in Figs. 8 and 9.

For total kinetic energy $TE \geq 203$ MeV, the surviving mass numbers are A=104-106, among which there are 16 even and 8 odd mass numbers; therefore $\delta A=30$ %. For $TE \geq 200$ MeV J. Trochon et. al. [14] measured mass number and proton number distributions. From their results one obtains $\delta A \cong 20$ %; $\delta Z \cong 60$ %, and $\delta N \cong 60$ %.

The mass number distribution in the window of light fragment kinetic energy E = 112 MeV, in $^{239}\text{Pu}(n_{th},f)$, obtained by C. Schmitt et. al., is presented in Fig. 10 [15]. From this data one calculates $\delta A \cong 3.7$ %. For this energy they obtain $\delta Z \cong 15$ %, and $\delta N \cong 10$ % [15]. For E > 119 MeV, one obtains the distribution presented in Fig. 11, from which one calculates $\delta A = 7.6$ %. Suppose that for E > 119 MeV, the proton numbers correspond to Z_0 , therefore $\delta Z = 66.6$ % and $\delta N = 33.3$ %, which are coherent with the stereographic projection of the values obtained by C. Schmitt et. al., for lower energy windows. See Figs. 12 and 13.

For TE > 210 MeV, one obtains masses $104 \le A \le 107$, with the higher yield corresponding to A = 106.

For lower kinetic energy windows, one obtains $\delta A = 0$. This result does not imply that δZ y δN values are zero. M. Montoya et. al. using a combinatorial analysis demonstrated [9] that if there is one and only one nucleon (proton o neutron) pair breaking, then

$$1 + \delta A = \delta N + \delta Z. \tag{1}$$

H. Nifenecker *et. al.* [16] developed other combinatorial analysis that produces the same relation.

III. SHELL AND COULOMB EFFECTS ON COLD FISSION

In cold fission from $^{233}\text{U}(n_{th},f)$, $^{235}\text{U}(n_{th},f)$ and $^{239}\text{Pu}(n_{th},f)$, shell and Coulomb effects on mass number and kinetic distribution were observed [9].

To describe "Coulomb effect" let's first define the following curves depending of A: i) \tilde{Q} , the smoothed curve referred to maximal value of available energy of the reaction (Q), as a linear curve in the mass region from the lightest A to that at which ends the linear trend and, for higher mass numbers, a curve following the approximately horizontal trend of Q; ii) C, the electrostatic interaction energy between complementary spherical fragments corresponding to Z_0 , with surfaces separated by 2 fm (the result is a step function of mass number); and iii) K, the maximal value of total kinetic energy, as the lowest of the ten highest values of total kinetic energy, defined as presented by M. Montoya for $^{233}U(n_{th},f)$, $^{235}U(n_{th},f)$ and $^{239}Pu(n_{th},f)$, respectively [17].

Now let's define the smooth excess of electrostatic energy, as a function of A, by the relation

$$\delta C = C - \tilde{Q} \tag{2}$$

and the smoothed values of minimal excitation energy, as a function of A, by the relation

$$X = \tilde{Q} - K \tag{3}$$

The curves of C, K, and \tilde{Q} values for $^{233}\mathrm{U}(\mathrm{n}_{th},\mathrm{f})$ are presented in Fig. 14.

The fluctuations of K in $^{233}\text{U}(n_{th},f)$, $^{235}\text{U}(n_{th},f)$ and $^{239}\text{Pu}(n_{th},f)$ are interpreted as effects of the step variation of the electrostatic energy as a function of Z_0 [17, 18].

It is found that the smoothed values δC and X are correlated. This result suggests that, at scission, a higher excess of electrostatic interaction energy produces a higher deformation of fragments, therefore a higher X and A then lower K-values.

For the mass regions 78 $\leq A \leq 100$ in $^{233}\mathrm{U}(\mathrm{n}_{th},\mathrm{f})$; 80 $\leq A \leq 102$ in $^{235}\mathrm{U}(\mathrm{n}_{th},\mathrm{f})$; and 90 $\leq A \leq 108$ in $^{239}\mathrm{Pu}(\mathrm{n}_{th},\mathrm{f})$: δC and X are decreasing functions of A. See Figs. 15, 16 and 17.

In 233 U(n_{th},f), the higher Q-values, are around 204 MeV, which occurs in the mass region $100 \le A \le 106$, which corresponds to the lowest values of δC . See Fig. 15. For complementary fragments (Z = 50, N = 80) and (Z = 42, N = 62), the K value reach the respective Q value.

As it is presented in Fig. 16, in the mass region $100 \le A \le 106$, in $^{235}\text{U}(n_{th},f)$, δC well as X are very approximately zero.

 $In^{239}U(n_{th},f)$, the lowest X value occurs in the mass region $100 \le A \le 110$. See Fig. 17.

For 233 U(n_{th},f), 235 U(n_{th},f) and 239 Pu(n_{th},f), the value of δC is not zero. At least one of the fragments must be deformed and spends energy for that. However, molybdenum (Z=42) with N=60, 62 y 64; and zirconium (Z=40) with N=60, 62 y 64; have prolate geometries in their ground states, in addition they are transitional and soft [9]. At scission, these fragments are deformed without excitation energy, and the electrostatic energy is equal to the Q-value.

For $^{233}\text{U}(n_{th},f)$, $^{235}\text{U}(n_{th},f)$ and $^{239}\text{Pu}(n_{th},f)$, the fluctuations of mass number yield are anti-correlated to δC [6, 7].

For 233 U(n_{th},f), in the light fragment kinetic energy window $113.5 \le E \le 114.5$ MeV, the mass yield peaks toward a maximum around A = 90 and 100, respectively, which correspond to minimal values of δC [9, 16]. For 235 U(n_{th},f), in the light fragment kinetic energy window $113.5 \le E \le 114.5$ MeV, the mass yield peaks toward a maximum around A = 90 y 102, respectively, which correspond to minimal values of δC . For 239 Pu(n_{th},f), in the light fragment kinetic energy region E > 118 MeV, the mass yield peaks toward a maximum around A = 84, 89, 96, 100 and 106, respectively, which correspond to minimal values of δC .

For $^{233}\mathrm{U}(\mathrm{n}_{th},\mathrm{f})$ as well as for $^{235}\mathrm{U}(\mathrm{n}_{th},\mathrm{f})$, for E>106, δC increases sharply with A and, therefore, K decreases sharply too. For the reaction $^{235}\mathrm{U}(\mathrm{n}_{th},\mathrm{f})$, δC decrease for A>110.

The fluctuations of X and δC are correlated and they increase with asymmetry of fragmentations. This is because the step-variation of the electrostatic interaction energy between fragments produced, by changing a unit of proton number, is more pronounced in asymmetric region, as one may in Fig. 17, corresponding to 233 U(n_{th},f).

The electrostatic interaction energy between complementary fragments constitutes a barrier to fission in the channel of the corresponding charge and mass. The probability to produce a couple of fragments will be higher for lower difference between this barrier and the available energy. Thus, for a same Q-value, between neighbor mass numbers, the

fragments with higher asymmetry of charge will reach higher values of kinetic energy. This is equivalent to say for TE close to the maximal value the prevalent fragmentations will be those with higher asymmetry. The Coulomb effects in cold fission will be present also in proton number yields corresponding to odd proton number. The higher yield corresponds to higher asymmetry, as it was shown by W. Schwab *et. al.* in the case of $^{233}U(n_{th},f)$ [19].

IV. CONCLUSIONS

Neutron emission has erosive consequences on fragment mass and kinetic energy distribution in $^{233}\text{U}(n_{th},f)$, $^{235}\text{U}(n_{th},f)$ and $^{239}\text{Pu}(n_{th},f)$. To avoid those disturbances, the cold fission, i.e. very low excitation region, was studied. Contrary to expected, in cold fission, nucleon pair breaking still exists. Nevertheless at the maximal total kinetic energy only even-even fragments survive. For lower energies, zero odd-even effect on mass distribution does not exclude non zero odd-even effects on proton or neutron distributions.

In addition, in cold fission, Coulomb effects on charge, mass and kinetic energy distribution are present: for two fragmentations with equal Q-value, the higher yield corresponds to the higher charge asymmetry. Moreover, Coulomb effects are presented as fluctuations of the maximal kinetic energy value as a function of mass. This effect is due to the fact that, each five units of mass number, there is a change of the proton number that maximizes the Q-value, which produces a step variation of electrostatic interaction energy between complementary fragments with the same shapes. A similar effect on mass number yield curve is observed. Due to the characteristics of electrostatic interaction, those effects are more notorious in higher asymmetry region. Finally, results from several experiments in cold fission suggest that scission explore all configurations permitted by the Q-value.

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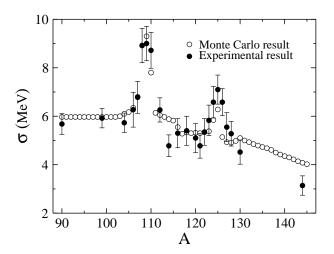


FIG. 1: Belhafaf *et. al.* experimental [2] and Monte Carlo simulation [4, 5] results on standard deviation of the kinetic energy distribution as a function of fragment mass number in the reaction $^{235}\text{U}(n_{th},f)$. See text.

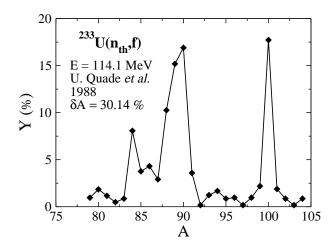


FIG. 2: Mass number distribution in the energy window E=114.1 MeV for cold fission from $^{233}\text{U}(n_{th},f)$. Taken from Ref. [10]. From these data one calculates $\delta A=30.14\%$. See text.

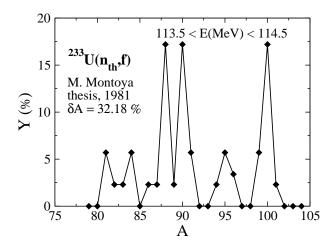


FIG. 3: Mass number distribution in the energy window 113.5 < E < 114.5 MeV for cold fission from $^{233}\text{U}(n_{th},f)$. Taken from Ref. [9]. From these data one calculates $\delta A = 32.18\%$. See text.

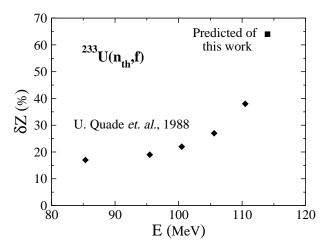


FIG. 4: Odd-even effects on the proton distribution as a function of E in $^{233}\text{U}(n_{th},f)$. Values are taken from Ref. [11], except the higher one, which corresponds to prediction of this work. See text.

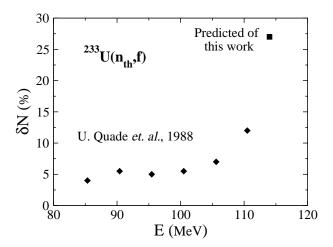


FIG. 5: Odd-even effects on the neutron distribution as a function of E in 233 U(n_{th},f). Values are taken from Ref. [11], except the higher one, which corresponds to prediction of this work. See text.

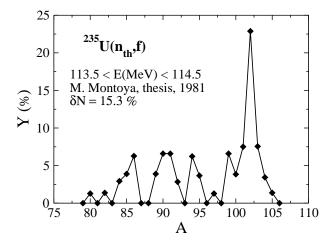


FIG. 6: Mass number distribution in the energy window 113.5 < E < 114.5 MeV for cold fission from $^{235}\text{U}(n_{th},f)$. Taken from Ref. [9]. From these data one calculates $\delta A = 15.3\%$. See text.

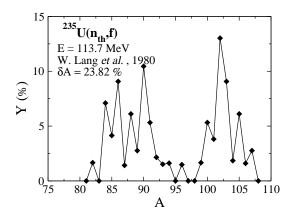


FIG. 7: Mass number distribution in the energy window E = 114.5 MeV for cold fission from the reaction $^{235}\text{U}(n_{th},f)$. Taken from Ref. [12]. From these data one calculates $\delta A = 23.82\%$. See text.

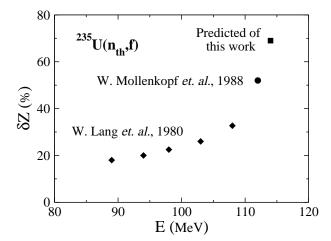


FIG. 8: Odd-even effects on the proton distribution as a function of E in $^{233}\text{U}(n_{th},f)$. Values are taken from Ref. [12] and [13], except the higher one, which corresponds to prediction of this work. See text.

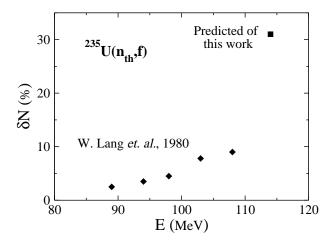


FIG. 9: Odd-even effects on the neutron distribution as a function of E in $^{235}\text{U}(n_{th},f)$. Values are taken from Ref. [12], except the higher one, which corresponds to prediction of this work. See text.

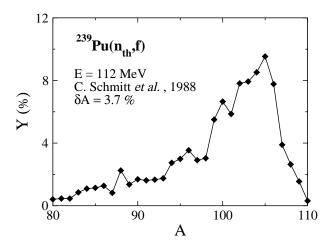


FIG. 10: Mass number distribution in the energy window E=112 MeV for cold fission from 239 Pu(n_{th},f). Taken from Ref. [15]. From these data one calculates $\delta A=3.7\%$. See text.

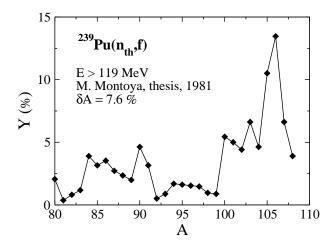


FIG. 11: Mass number distribution in the energy window E > 119 MeV for cold fission from 239 Pu(n_{th},f). Taken from Ref. [9]. From these data one calculates $\delta A = 7.6\%$. See text.

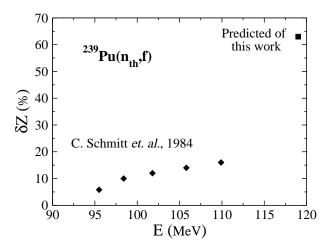


FIG. 12: Odd-even effects on the proton distribution as a function of E in 239 Pu(n_{th},f). Values are taken from Ref. [15], except the higher one, which corresponds to prediction of this work. See text.

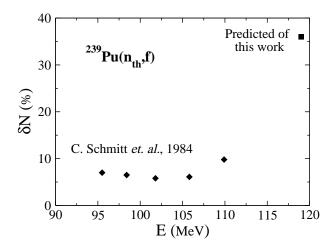


FIG. 13: Odd-even effects on the neutron distribution as a function of E in 239 Pu(n_{th},f). Values are taken from Ref. [15], except the higher one, which corresponds to prediction of this work. See text.

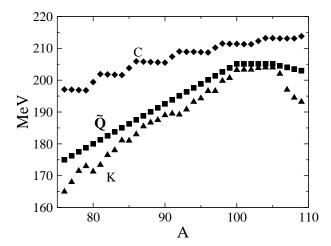


FIG. 14: Electrostatic interaction energy between spherical fragments with spherical surfaces separated by 2 fm(C); smoothed curve of maximal available energy (\tilde{Q}); and maximal value of the total kinetic energy (K) for 233 U(n_{th},f). See text.

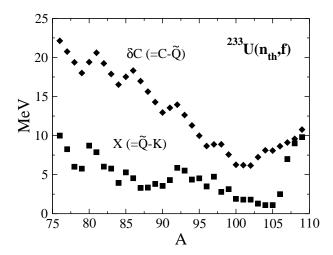


FIG. 15: Smoothed curves of electrostatic energy excess δC (= $C - \tilde{Q}$) and minimal values of total excitation energy X (= $\tilde{Q} - K$), a function of light fragment mass number A in $^{233}\mathrm{U}(\mathrm{n}_{th},\mathrm{f})$. See text.

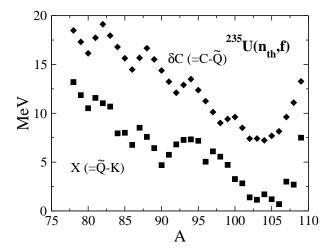


FIG. 16: Smoothed curves of electrostatic energy excess δC (= $C - \tilde{Q}$) and minimal values of total excitation energy X (= $\tilde{Q} - K$), a function of light fragment mass number A in $^{235}\text{U}(n_{th},f)$. See text.

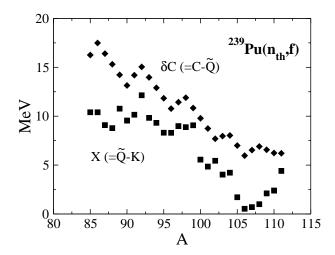


FIG. 17: Smoothed curves of electrostatic energy excess δC (= $C - \tilde{Q}$) and minimal values of total excitation energy X (= $\tilde{Q} - K$), a function of light fragment mass number A in 239 Pu(n_{th},f). See text.